Design of 2-Hinged Spandrel Braced Steel Arch Double Track Railway Bridge, 400 ft. Span

Samuel Klein E. O. Greifenhagen

1906

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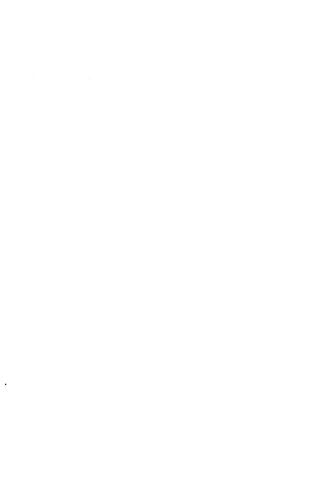
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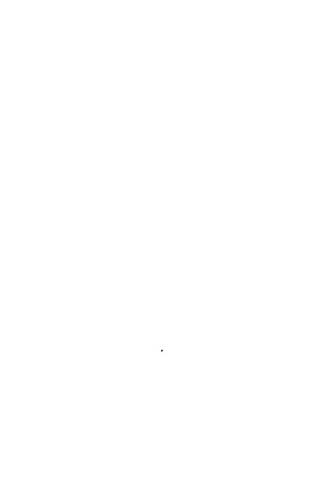


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AT 42 Klein, Samuel Design and general details of a 2-Hinged Spandrel

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DESIGN & GENERAL DETAILS

of a

T -AINGED SPANDREL BRACED STEEL ARCH

DOUBLE TRACK RAILWAY BRIDGE

400 foot SPAN

A THESIS presented by

Dannel Klein.

6. C. Greifenhagen, to the

President & Faculty

of the

Armour Institute of Technology

for the Degree

of

Bachelor of Science in Civil Engineering having completed the prescribed course of study in Civil Engineering.

Chicago

1906

ILLINOIS INSTITUTE OF TECHNOLOGY PAUL V. GALVIN LIBRARY 35 WEST 33RD STREET CHICAGO, IL 60616 Howard M. Raymond. Draw of Eng. Fludes

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The Theory of the Spandrel Braced Arch

The usual formula for the invariability of span of an arch $\frac{EF.DE}{EI} = C$ (Greene's Arches, Part III page 19)

is not applicable to the spandrel braced arch with horizontal

is not applicable to the spandrel braced arch with horizontal top chord. In the above equation, EF is the vertical

intercept between the equilibrium polygon AEB (for the load P) and the axis of the rib; and

DE is the vertical ordinate to the equilibrium polygon, E is the co-efficient of elasticity, which is

usually constant and may be taken outside of the summation sign. I is the moment of inertia of successive cross sections of the arch. In the braced arch this moment of inertia is variable and must be included in the summation; also, the values of this moment of inertia cannot be determined until the sections are known, and these two facts make it impracticable to apply this formula to the braced arch.

The omission of a center hinge renders the horizontal thrust at the abutments a statically indeterminate quantity. However, there are two practical methods of determining this thrust; lst, by the application of the theorem of "least work", and 2d, by the elastic theory.

Determination of H (First Method).

Application of the Theory of Least Work.

The following equations for determining H are taken from Mueller-Breslan's, "Statik der Bankonstruction", and Du Bois'. "Framed Structures".

In Fig. 1, let the span AB be equal to \(\alpha\), and let F

be the load at a distance KL from

the left end, where K is any given

fraction. Let \(\alpha\) DOTY be the co
ordinates of the center of moments

for any member where the moment is

M. Let \(\rho_A \) the lever arm of the

same member with respect to this center. Thus, for the member CD, the center of moments is O.

AB = \(\alpha\), The stress in any member is \(\frac{M}{R} \); and if we let \(\alpha\)

be the sectional area of the member, and \(\alpha\) its length, then



the worth of straining that member /s

The total work of straining all the members then is

$$\xi_{\rm H} = W = \underbrace{\frac{M^2}{2\pi^2 p^2}}.$$

Now, for any member to the left of F , we have $\mathcal{N} = \mathcal{H} V - \mathcal{P}_A = \mathcal{H}_A - \mathcal{P}_C - \mathcal{H}_A \lambda,$

and for any member on the right, we have

$$\mathcal{M}=\mathcal{H}_{\mathcal{Y}}^{*}-\mathcal{P}_{\mathcal{X}}^{*}+\mathcal{P}_{\mathcal{X}}^{*}-\mathcal{A}_{\mathcal{X}})=\mathcal{H}_{\mathcal{Y}}^{*}-\mathcal{P}_{\mathcal{X}}^{*}-\mathcal{A}_{\mathcal{X}}^{*}+\mathcal{P}_{\mathcal{X}}^{*}-\mathcal{A}_{\mathcal{X}}^{*})$$
 Substituting these values of \mathcal{M} in $\mathcal{E}_{\mathcal{Z}}$, we get

By the principle of least work, the total work W must be a minimum. Differentiating $E_{\mathcal{F}}(\mathcal{F})$ with respect to \mathcal{F} , and putting the first derivative equal to zero, we get the value of \mathcal{F} which will make the work \mathcal{F} , a minimum.

hence, since £ is constant,

$$\mathcal{H} = \frac{P(-n) \xi_{n}^{(n)} \lambda_{n}^{(n)}}{E^{(n)}} + F \xi_{n}^{(n)} (-n) \frac{\lambda_{n}}{E^{(n)}} - \lambda_{n} - h_{-}) \frac{\lambda_{n}}{E^{(n)}}}{\xi_{n}^{(n)}} \qquad (44)$$

Let S_o be the stress in any member due to a unit horizontal thrust at the abutment, and let S_o , be the stress due



to a unit load at \mathcal{P} . Then we have for any member to the left of \mathcal{P} ,

$$S_0 = \{ \gamma \}, \qquad S_0 = \{ \gamma \in \mathcal{T} \},$$
or $S_0 = \{ \gamma \}, \qquad S_0 = \{ \gamma \in \mathcal{T} \},$

Multiplying these two equations, we have, for any member on the left.

For any member to the right of F, we have

Hence for any member to the right of F.

Substituting $\overline{\mathcal{I}},\mathcal{E}_{\delta}$ for their above values in $\overline{\mathcal{I}},\mathcal{E}_{\delta}$ we get

$$H = P = \frac{\underbrace{\begin{cases} \frac{1}{2} \cdot \underbrace{\frac{1}{2} \cdot \frac{1}{2}} \\ \frac{1}{2} \cdot \underbrace{\frac{1}{$$

The above value for // is that derived by Du Bois, and as is seen, necessitates the computation of the stresses in all the members due to a unit load at each panel point. In practice this would prove to be very tedious work. A somewhat similar formula, but better adapted to practice, may



be obtained by slight changes in the foregoing expressions. as follows:

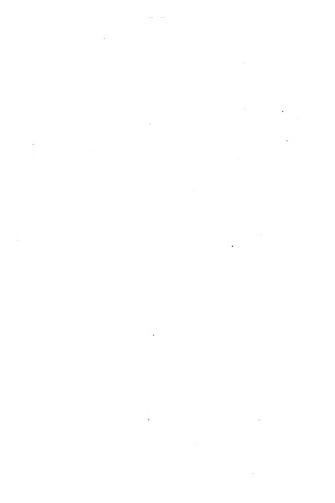
As before, for any member to the left of \vdash , we have

For the members to the right of -, we may consider the right abutment to be the origin of co-ordinates; or the load \nearrow may be assumed on the symmetrical panel point to the right of the center. The reaction at the left abutment on this assumption is, \nearrow = \nearrow //

So for these members

By substituting these values of Mafor / in Elect, we get

$$W = \begin{cases} \frac{1}{2} \frac{1}{2} \frac{1}{2} - \frac{1}{2} \frac{1}$$



As before, let \leq_{o} be the stress in any member due to a unit thrust at the abutment; but let \leq_{o} now be the stress in any member due to a unit vertical reaction at the abutment.

Then

$$C_{i} = \frac{\lambda_{i}}{\lambda_{i}}, \qquad C_{i} = \frac{\lambda_{i}}{\lambda_$$

By substituting these values in 54.60, we get

This is the value of H in a more useful form.

<u>Determination of H.</u> (Second Method)

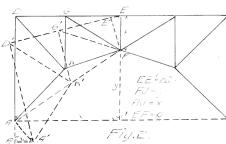
<u>Application of the Elastic Theory.</u>

This method was first given by Prof. Clerk-Maxwell in "The Cyclopaedia Britannica" and is presented in detail by Prof. Greene in his book on Arches. Mr. R. S. Buck gives the method in his paper on the Niagara Arch.



In the arch of FNC, let us consider the right end as fixed and the left end free to move. Now if we consider any member, as OC, as being strained due to a stress set up in that member, and if we assume no other member being strained, then the span of the arch will be changed by an amount $\triangle L$, which will be proportional to the horizontal thrust at the free end. This thrust, of course, is great enough to prevent all movement and by finding the amount of this possible movement we find the amount of the thrust which resists it.

In the case of the member $\mathcal{E}_{\mathcal{F}}$, the motion can be considered as taking place about the center \mathcal{F} , which is the center of moments



for the member being considered. We may now write

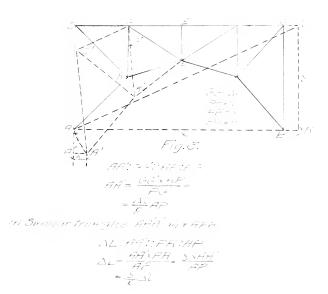
In similar Triangles HAH and HE,

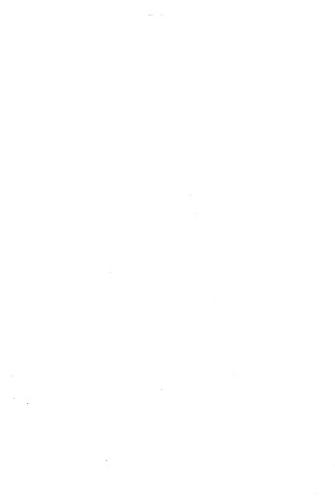


$$A_{ij} = \frac{1}{2} \sum_{j=1}^{n} A_{ij} = \frac{1}{$$

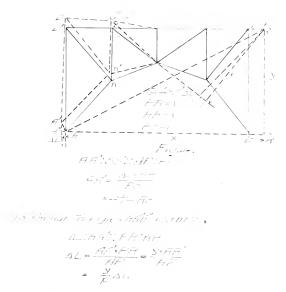
The distortion diagrams and the value of $\triangle \angle$ for a strain in a vertical post, in a diagonal, and in a rib member are given below:

VERTICAL POST:

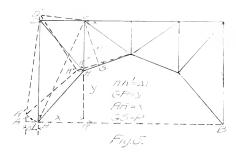


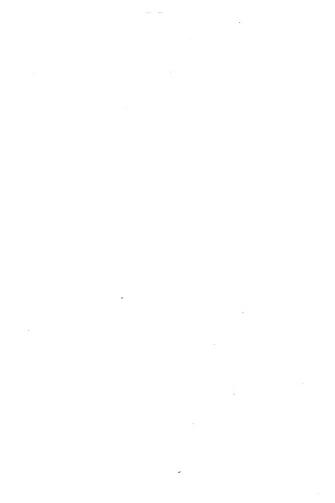


DIAGONAL BRACE:



RIB MEMBER:





In sumiar thousage AFA and Her

$$\Delta L: HA :: GH: AG$$

$$\Delta L = \frac{HA' \times GH}{AG} = \frac{Y \times HA'}{AG}$$

$$= \frac{1}{4} \frac{1}{$$

From Hook's Law

$$\Delta \vec{c} = \frac{T\vec{c}}{H\vec{E}} \,, \tag{5}$$

(7)

where

Tis the stress in a member,

E /s the co-officient of elasticity,

A is the cross-sectional area of the member,

the length of the member, and

Al isthechange in length, r strain due to stress. T.

Now by substituting the value of $\triangle C$ given in $E_{1}(C)$, for $\triangle C$ in $E_{2}(C)$, we get

$$\Delta L = \frac{I}{EA} \frac{Zy}{p}. \tag{9}$$

Any reaction at the abutments having horizontal and vertical components,// and /, will produce a stress, /, in any piece which will give, by the method of moments

$$T = \frac{HY + F - x}{P} .$$
 (10)



By substituting this value of T in Z we get

The above quantity may be calculated to give the movement of the free end due to the deformation of each member of the truss. The error introduced due to the slight yielding of all the other members at the same time is inconsiderable as long as there is no sensible change in the outline of the truss.

The total change of span will then be the sum of the changes due to each member. or

Now the abutments do not yield and the span remains constant, hence $2\Delta \Delta$ must be zero.

So, from Equilibrium have, by solving for H,

The above value for $\mathcal H$ is the same as that given in Eaux and derived by the other method.

In the Engineering Record, Vol. 46, page 435,is given a simplified formula for $\mathcal H$ as derived by Mr. General Aus and approved by Mr. Theodore Cooper, Convolting Engineer. The modification is obtained by developing the formulae for $\mathcal H$ for two symmetrical penels and submarizing them. After finding the value of $\mathcal P$ for one or two symmetrical members for each loading, the value of every other $\mathcal H$ for any sember can be written out mechanically, as these values have an easily established relation to each where. The submart on of the values of $\mathcal H$ for any particular load gives the total $\mathcal H$.

abutment lue to the load / on

the arch and // is the horizontal thrust lue to a stress in the one member considered alone. Here lies the first error; the // used in the formula must equal the total // due to stresses in all members, or, in other words, due to the load $\mathcal P$. If it were possible to find the vortical reaction due to the one member alone, then the corresponding // due to this member could be used; but I' being the total vertical reaction, then $\mathcal P$ must also be the total horizontal thrust actually at the abutment and due to the stresses in all the members.



However, overlooking Ar. Aus's error, let us follow him farther in his derivation of \mathcal{A} .

now since the abutments are fixed $\triangle \sqrt{c}$ must equal zero, and solving Eq. (/), we get

and then the total ${\mathcal H}$ due to stresses in all the members is

At first glance, notwithstanding his error, Mr. Aus apparently derives the correct value of $\not i$.

But he is here guilty of another error in writing

instead of

In other words Mr. Aus boldly states that the summation of a series of fractions equals the summation of the numerators divided by the summation of the denominators.



Returning to equation (:),

Mr. Aus assumes as a first approximation that the areas and lengths of all the members are equal. Hence he writes

Therefore

If Eq. (\tilde{z}) is correct there is no need of <u>assuming</u> the lengths and areas equal. We can write at once,by cancelling from the fraction,

This is Mr. Aus's simple formula.

To sum up this criticism; Mr. Aus does not dispute the correctness of Prof. Greene's formula, and apparently derives it, but in the application of his own formulas to the design of the Rio Grande Arch he actually gets $\mathcal{A} = \underbrace{<}_{\mathbf{S}_{\mathbf{G}}} \underbrace{<}_{\mathbf{S}_{\mathbf{G}}}$,

which he states equals $\frac{\xi - \xi_0 + \frac{2}{2} R}{\xi - \xi_0 + \frac{2}{2} R} V$.



The Conjutation of Stresses

in a

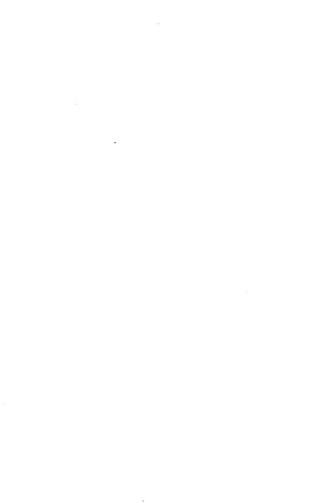
400 foot Railway Arch.

The arch is of the spandrel braced type lith two hinger. The lower chord, r rib,i: parabolic in form and the upper chord is horizontal, and the two chords are braced together by a system of vertical and diagonal web members. The span of the arch, seasured between centers of the end hinges, is four hundred feet (400 feet) and is divided by the vertical posts into sixteen panels of twenty-five feet (25 feet) each. The trusses lie in planes battered one in eight (1 in 2) to the vertical. Heasured in the plan of the truss, the rise of the rib is eighty feet (80 feet) and the depth of the truss at the crown is twelve feet (10 feet).

Stresses due to Live Vertical Loads.

A moving load of 6000 pounds per lineal foot of track was assumed, making the concentrations at panel points 150,000 pounds, or 150 kips.

Equation (10),on page (11), gives us the stress in any member due to a panel load W^{\prime} as



"s can readily find the vertical reaction. A, in any case, but we is not so easily obtained. To get its value me must use the formula riven on page 11;

$$\mathcal{H} = \frac{F(\mathcal{L}_{p,p}^{m}) + F(\mathcal{L}_{p,p}^{m}) + F(\mathcal{L}_{p,p}^{m})}{\mathcal{L}_{p,p}^{m} + \mathcal{L}_{p,p}^{m}} \cdot \frac{\lambda_{p,p}^{m}}{\mathcal{L}_{p,p}^{m}} \cdot \frac{\lambda_{p,p}^{m}}{\mathcal{L}_{p,p}^{$$

It is seen from this formula that the values of the sectional areas of the members are necessary to get a correct value of \mathcal{H} . As a first approximation these areas were assumed to be equal and the expression \mathcal{H} dropped out of the formula. It was now necessary to get the expressions

In order to get these values a table was constructed, and the work was systematized. This table is shown on PLATE $\overline{\mathbf{I}}$. To begin with, the values of $\overline{\mathcal{I}}$, $\overline{\mathcal{I}}$,



obtained analytically. It is noted to the sign of $\frac{\lambda}{C}$ is plus for the upper chord and vertical to bord, not negative for the lower chird and diagonal vertical to the sign of $\frac{\lambda}{C}$ is plus for lower chard merbers, and negative for the upper chord and vertical nembers. The sign of $\frac{\lambda}{C}$ is glue in all the diagonal members except, $\frac{\lambda}{C} = 2$, here it has a single sign. The sign of $\frac{\lambda}{C}$ is plaus in our cases with the sign of this diagonal, $\frac{\lambda}{C} = 2$. The values of $\frac{\lambda}{C} = 2$ where

Referring again to FLATH I, in the column headed $\frac{\partial}{\partial x} \partial x$ are tabulated the products of the quantities $\frac{\partial}{\partial x} \partial x$, where, for each member. The next column contains the survations of these products from this left end of the trues up to each member in turn. These summations are grouped according to the type of the member, thether upper of rd, lower chard, diagonal, or vertical. The next column is headed $\frac{\partial x}{\partial x} \partial x$, and contains these quantities, and their total sums, the partial summations not being required in the formula.

The right half of PLATE I has three divisions corresponding to three determinations of the value of //, and each division has eight subdivisions, one for each panel point which may be loaded. The loft hand column in these small subdivisions contains the values of $\sqrt{\frac{n-\lambda_1}{\lambda_1}} Z$,



(the summation for all members ich), we thele center of moments lying to the left of the product condition on the left hand column contains the order of 2, 2 × 4 × 6 (the summation for the members which have their center of momentallying to the right of the loaded panel point).

These columns are added to give the total for all four types of members and then these totalware multiplied by Francis, to give Francisco for the value of Francisco for the current these two products divided by the value of Signature of Francisco for the value of Francisco for the

To explain the details of the method or re-definitely, we will illustrate by a specific instance. In the division for the first value of \mathcal{H} consider the small table headed, "Load on $\underline{\mathbf{5}}$ ". The first when in the left hand column, 600.831, is the value of $\mathbf{5}$ for all the upper chard members from $\mathbf{6}$ — $\mathbf{6}$ up to and including $\mathbf{6}$ — $\mathbf{6}$. The next $\mathbf{6}$ bec,450.053, is the value of this summation for lower chard members from $\mathbf{6}$ — $\mathbf{6}$, to $\mathbf{6}$ — $\mathbf{6}$; next 403.604 is the summation for the diagonals from $\mathbf{6}$ $\mathbf{6}$ $\mathbf{6}$ $\mathbf{6}$ is the summation for the verticals from $\mathbf{6}$ $\mathbf{6}$ $\mathbf{6}$ $\mathbf{6}$ $\mathbf{6}$ is the summation for the verticals from $\mathbf{6}$ $\mathbf{6}$

is 10,746.043. This is the value of the surmation, $\leq_{c}^{l-m} \frac{XY}{D^{2}} c$,



wint. The form the summent of the bound of the right.

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There are the summent of the summer of th

For a load W on panel wint $\frac{5}{5}$ we have , $F_1 = \frac{14}{6}H_1$, and $F_2 = \frac{14}{6}H_2$. $E_3 = \frac{14}{6}H_3$, and the formula

becomes

H= 16W *1806.961+96W* [6,811.88]



Wich can be written

The purnities in the meananth are allefelent for each is but the denominator is constant and equal to 507,919.760. As μ is equal to 150 bits, is value of each H in hips is very readily obtained.

PLATE III gives the values of min, fix, and thirth for each member for a load on each years print. The values of min and make for a load on each years print. The values of min and min and their algebraic sum will be either plus or minus. By adding all the values of min and their plus or minus. By adding all the value of the maximum tension in any member due to loads on the particular panel points which give plus values. In the same way, by adding all the streams due to loads on panel wints which give minus values, we get the maximum compressive stream in a member. Those maximum streams in each member are then combined with the streames due to doad load. Wind, and temperature, and the maximum maximum streams in the member to thus obtained. (The method of obtaining these other streams and making the combination will be described later).

Having the maximum stress in the members, we divided by an assumed unit stress of 10,000 pounds for square inchand



chtained approximate area. These then pere tabul too on PLATE 1 in the first of the first orbit is seed "revised areas". In the next column, under this heading, riven the values of the first proceeding ordina the values of the first proceeding ordina by the value of that particular member. Values of the area are also obtained by dividing the proceeding values of the py the values of the theorem. The same betted, as is described above, is

PLATE IV contains a table with the values for $\mathcal{H}_{\lambda}^{A}$,

then worked through to rive the separate values for A.

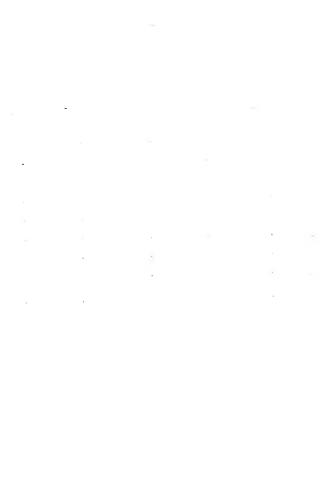
and $F_{\mathcal{L}}^{A}$, and $F_{\mathcal{L}}^{A}$ for these revised values of H. The values of $F_{\mathcal{L}}^{A}$ remain the same as an PLATE III, but the values of $F_{\mathcal{L}}^{A}$, and the sum $F_{\mathcal{L}}^{A}$, and of course change, and the rexisum positive and negative stresses are altered. These new maximum values combined with the dead load, in , and temperature attractor give new maximum maximorum values for the strenges; and these are the values which were used in the final decime.

These actual areas were wood to obtain a third set of values for ${\mathcal M}$. The work for this determination is also shown on PLATE I.



Below is given a list of the three set, of Indevidual and total H's with their differences:

Load on	Hs-I areas equal	Diff.	Hs-II revised areas	Diff.	Hs-III actual areac
1	.1698	0064	.1634	0006	.1628
5	.3349	0140	.3207	.0014	.3201
8	.4663	.0045	.4708	.0082	.4790
4	.6099	.0028	.6107	.0064	.6191
5	.7390	.0025	.7415	.0098	.7513
6	.8341	.0184	.8525	.0131	.8656
7	.914?	.0227	.9374	.0206	.9580
8	.9448	.0180	•9628	.0351	.9879
Full Load	9.0822	.0784	9.1606	.1431	9,3037



Stresses due to Dead Vertical Loads.

The dead weight of the bridge was assumed to be 10,000 pounds per lineal foot, making 5,000 pounds per foot of truss. This gives a panel load of 125,000 pounds or 125 kips. 80 per cent or 100 kips concentrated on the upper chord and 20 per cent or 25 kips on the lower chord. In getting the dead load stresses the assumption was made that the truss had been given a camber sufficient to give the lower chord its parabolic form when under the deflection due to a uniform dead load. This camber is obtained by changing the length of each member by a definite calculated amount. With this assumption made the panel loads may be considered as transferred directly to the lower chord through the posts, causing stress in the lower chord members and posts only. The lower chord stresses are readily found by the graphical method and the stresses in the posts equal 80 per cent of the panel load or 100 kips.

Stresses due to Wind Loads.

Steady Wind Loads.

The steady wind load was assumed to be nine pounds per square foot of truss area, one-half to go to each chord.

The one-half on the lower chord is divided equally between the two trusses bracing (between ribs). The part of the load on the upper chord is transferred by the sway bracing to the lower chord of the wind-ward truss. These horizontal wind loads were different at each panel point due to the different depths of the truss. On PLATE II is shown the developed plan of the lower lateral system and the stresses produced by the steady wind.

The horizontal steady wind load on the upper chord is equivalent to an equal horizontal load on the lower chord plus a moment about the lower chord panel point. This moment is equal to the load on the upper chord times the vertical height above the lower chord. By dividing this product by the distance between trusses at the lower panel points a vertical force is obtained, acting down on the leeward side and up on the windward side. These vertical overturning forces cause stresses in the trusses and must be considered.

The panel points of the lower chord do not lie in the same horizontal plane and therefore the wind loads at these points will also cause overturning moments equal to that of definite equivalent vertical forces at the panel points. The method of obtaining these <u>equivalent vertical forces</u> is described in Merriman & Jacoby, "Higher Structures" Art. 71 page 193.

These two vertical forces acting at each panel point



were added and their values expressed in kips. Now in the table on PLATE III are given the stresses in all members due to a load of 150 kips on each panel point. Of these stresses be multiplied by the ratio of the vertical forces to this load of 150 kips the stresses in the members due to these vertical forces can be obtained. PLATE V contains a table showing the stresses due to the vertical forces obtained in this manner.

Live Wind Stresses.

The live wind stresses are due to the wind on the surface of trains and are assumed to be taken by the upper lateral system. The pressure on the trains is taken as 400 pounds per lineal foot or 10 kips per panel. The upper lateral system is designed as an ordinary truss with parallel chords with loads of 10 kips at the panel points. These wind loads on the train also cause overturning moments on the truss. The amount of these horizontal wind forces (10 kips) multiplied by the vertical distance of their point of application above the lower chord this product divided by the distance between the lower chords at the panel points considered gives the value of the equivalent vertical forces due to the live wind. The ratio of these forces in kips to the panel load of 150 kips multiplied into the stresses due to

1

to a second

. G

these loads of 150 kips gives the stresses due to the live wind overturning forces. These stresses are tabulated on PLATE V.

It is to be noted that the equivalent vertical forces due to the overturning moments of both live and dead wind loads act downward on the leeward truss and are applied on the lower chord. The stresses due to the live vertical loads of 150 kips are calculated on the assumption that the loads are applied on the upper chord and since the stresses due to the vertical forces caused by wind are obtained directly from the former stresses, there must be a correction made to allow for this difference in the point of application. The correction is made in the stresses in the posts by adding a positive stress equal to the panel load at that post algebraically. All these stresses as finally obtained are true for the leeward truss only. The stresses in the windward truss will be equal in amount but opposite in sign.

Temperature Stresses.

Variations in temperature tend to produce changes in the lengths of the members of a truss and since these changes

cannot freely take place in the case of a two-hinged arch stresses will be set up in the members. Changes in the lengths of the members would cause a change in the span of the arch and the amount of this change would depend on the length of span, the range of temperature, and the co-efficient of expansion of steel. Now since the abutments are fixed the span cannot alter, but the tendency to do so will cause a thrust or pull which we will call $M_{\rm f}$. We can determine the value of this $M_{\rm f}$ and by the method of moments easily get at the resulting stresses in the members, which we call the temperature stresses.

Referring to page 10 we find Equations

now is we let all the symbols have the same significance but consider ${\mathcal T}$ the stress in the member due to the temperature we have

and substituting in the former expression we get

the total change in span is

but $\lesssim_{1/2}$ is equal to $7\varepsilon_{1/2}$ where 7 is the change in



temperature in degrees, $\mathcal S$ is the co-efficient of linear expansion, and $\mathcal L$ is the length of span in feet, therefore

solving for the we get

Now for the first approximation, where the areas were all considered equal, we assumed $\mathcal A$ to equal about 196 square inches and found the value of $\mathcal H$ as follows:

the value of $\lesssim \frac{1}{\sqrt{2}} \mathcal{J}$ is given as 12,995 on PLATE I.

The value 85.5 kips multiplied by \geq for each member gave the stresses in the members due to temperature. In the revision of areas the value of the summation $\leq \frac{1}{2\sqrt{27}}$ was known as 83.492 in by substituting this value in the above expression for f_{ℓ} , the other quantities being the same,

we obtained 67.72 kips as the thrust or pull due to temperature, and this value gave us the stresses which were used in getting the final areas.

It is to be noted that temperature stresses are either plus or minus depending on the way the temperature varies.



A range of 75% either way from 50% was provided for.

Combination of Stresses.

The combining of the various stresses to give the final maximum values for which the members were designed was a rather difficult matter. The live load stresses and the dead load stresses were kept separate and the former was assumed to have twice the intensity of the latter. This assumption was introduced by adding one-half of the dead load stress to the live load stress and designing the member for live load, that is, by using unit stresses for live load.

The stresses in members due to vertical loads and temperature are the same in each truss but the stresses due to wind loads are opposite in sign in the two trusses. This latter fact made it necessary to consider the direction of the wind, and it is of course obvious that only those stresses obtained with the wind acting in the same direction can be combined.

In the lower part of the tables on PLATES III and IV are a number of rows containing the total stresses in each member due to the various causes. The first two rows marked Live Load — and Live Load — contain the maximum tension and



compression, respectively, produced by the vertical moving The next row, marked Dead Load, contains the maximum stress caused by the dead weight of the bridge. The two rows following are lettered Live Wind - and Live Wind and contain the maximum tension and compression, respectively, due to the equivalent vertical forces of overturning moment of the wind on the moving trains (live wind) in the members of the leeward truss. In the row entitled Steady Wind are given the stresses in the leeward truss due to the equivalent vertical forces of overturning moment caused by wind on the truss (steady wind). The two succeeding rows marked Wind Load -- and Wind Load -- contain the stresses in the top and bottom chords due to the part they play in the upper and lower lateral systems. These stresses are live in the case of the upper chord. The first row marked + gives the chord stress for loads on the same panels which gave the other maximum positive live stresses. The second row marked gives these chord stresses for loads which gave the other maximum negative live stresses. These two rows contain dead stresses in case of the lower chord members. The first row refers to the leeward truss and contains positive stresses and the second row refers to the wind-ward truss and contains negative stresses. The row labelled Temperature contains stresses which may be either plus or minus depending on the way in which the temperature varies.

The last five rows in this table are pretty well

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explained by their titles. Attention is called, however, to the fact that these maximum positive and negative stresses are not absolute maximums taken by themselves, but that they will give the <u>absolute</u> maximum maximum when combined.

A systematic method was used to get at the four stresses which give the largest total when combined. Eight cases were worked out for each number as follows; the maximum positive live load stress, the maximum negative live load stress, the maximum positive dead load stress and the maximum negative dead load stress, for both leeward and windward trusses.

If there is a reversal of stress in a member, that is, if the member alternately takes tension and compression the member is designed for a stress equal to the larger plus eighty per cent of the smaller.



Below are given numerical examples for one upper chord member and one posts to make clear how the maximum values were obtained.

UPPER-CHORD MEMBER 4-4.

Live Load Tension

Leeward Truss.

Live Load Compression

Live Load -	√ 433,53	Live Load - 805.10
Live Wind -	≠ 32.60	Live Wind- -70.50
Wind Load →	≠ 92.00	Wind Load - ≠160.00
	≠558.13	-715.60
Dead Load	Tension	Dead Load Compression
Steady Wind	-77.10	Steady Wind77.10
Temperature	<u> +201.00</u>	Temperature -201.00
	≠123.90	- 278.10
hetane-half dea	i plus live	$\frac{\text{tension}}{2} = \frac{123.90}{2} + 558.13 = 620.08$
θne-half dea	d plus live	compression = $\frac{278.10}{715.60} = 854.65$



Time Took Tomoson

Windward Truss.

Time Tood Comemogation

Live Load	rension	Live Load C	ompression
Live Load+	- / 433.53	Live Load-	-805.10
Live Wind→	- 32.60	Live Wind-	/ 70.50
Wind Load-/-	- 92.00	Wind Load	-160.00
			-894.60
Dead Load	Tension	Dead Load C	Compression
Steady Wind	→ 77.10	Steady Wind	-77.10
Temperature	7 201,00	Temperature	-201.00
	→ 278.10		-123.90

One-half dead plus live $\frac{\text{tension}}{2} = \frac{278.10}{2} - 308.93 = 448.43$ One-half dead plus live $\frac{123.90}{2} + 894.60 = 956.55$

From these figures it is readily seen that to get the greatest stress we must add eighty per cent of the greatest tension (which is 620.08) to the greatest compression (which is 956.55).

 $956.55 - .80 \times 620.08 = 1452.55$

1452.55 kips is the maximum maximorum stress for which the member is designed.



VERTICAL MEMBER 4.4

Leeward Truss.

Live Load → +84.50 Live Load - - 325.92

Live Load Compression

Live Load Tension

Live Wind -7.10	Live Wind - 22.30
÷ 91.60	- 348.22
	Wind Load at Vertical / 12.10
	-336.12
Dead Load Tension	Dead Load Compression
Dead Load100.00	Dead Load -100.00
Steady Wind- +9.80	Steady Wind \rightarrow 9.80
Temperature <u>≠68.20</u>	Temperature <u>- 68.20</u>
- 22.00	-158.40
One-half dead plus live	$\frac{\text{tension}}{2} = \frac{22.00}{2} + 91.60 = 80.60$
One-half dead plus live	$\frac{\text{compression}}{2} = \frac{158.40}{2} + 336.12 = 415.32$

Windward Truss.

Live Load Tension	Live Load Compression
Live Load + +84.50	Live Load - 306.00
Live Wind \neq - 7.10	Live Wind- 7.00.30
→ 77. 4 0	-305.83 Wind Load at Vertical + 10.13
	-715.72

Lead Load Tension	Lead Load Com-ression
_ead Load -100.00	Dead Load -100.00
Steady Wind - 0.80	Steady Wind - 9.90
Temperature - 68.50	Temperature <u>68.20</u>
- 41.60	- 178.00

one-half dead plus live tension =
$$\frac{-41.60}{2} \neq 77.40 = \pm 56.60$$

one-half dead plus live compression = $\frac{178.00}{2} \neq 315.72 = 404.72$

Combining the greatest compression (415.70) in this case with 80 per cent of the greatest tension (80.60) we get the maximum maximum in this case.

 $415.30 + .80 \times 80.60 = 479.80$ kips.

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In the above example of the lost \mathcal{GL}_{μ} it is noted that the stress 10.10 kips due to a live wind load at the vertical is alded to get the maximum compression. The maximum compression due to live wind is obtained for a load including this panel point, therefore, this stress must be added, but the tension due to live wind is obtained for a load <u>not</u> including this panel point, therefore, the stress is not added in the case of the maximum tension.

The maximum stresses in lower-chord members and diagonals were obtained in the same wey as they were in the case of the two types of members which have been illustrated.

Certain conventional signs have been used to indicate which stresses were used to get the various maximums. Referring to PLATES III & IV, we notice a small P_i/N or IV placed after some of the members. The letter P indicates that the <u>positive value</u> of the stress was used in obtaining the maximum <u>tension</u> and -P means that the <u>negative value</u> of the stress was used in thing the maximum <u>tension</u>. The letter N means that the <u>negative value</u> of the stress was used in obtaining a maximum <u>compression</u> and +N indicates that the positive value of the stress was used in getting the maximum <u>compression</u>. A letter M after a maximum stress shows that it was obtained in the <u>windward</u> truss. A letter N in this case means that there was no wind. The absence of a letter means that the legward truss is considered.



Design of a 400 Foot Railway arch.

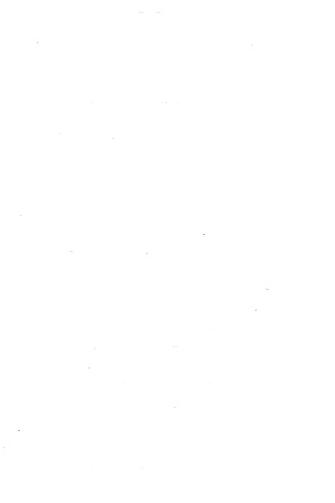
Main Truss Lambers.

In the design of the bridge, "Cooper's lactifications for Railrand Bridged" were followed with but few enduptions. All the main trust members were built up of plates and angles. In the case of the chirds and verticals the angles were placed outside of the webs and the cover plate was used, the other side being laced. In the diagonals the angles were turned in and a diaphren was used. The lower-chard was spliced to make up practically the full strength of the member and the upper-chard was apliced to provide for the greatest possible tension. The gusset plates at the joints were shop riveted to the upper end of the posts and to the and away from the abutment on the lower-chard members. An allowance of twenty per cent was made for field riveting.

PLATE VI gives the composition of the members and FLATE VII shows the details.

Floor System.

The details of the floor system may be found on PLATE VIII. Cooper's "E 50" concentrated engine leading was used



in the design of the stringer and floor-born. The living reare 45 inches dary and rest in the top "langer of the floor beams. The floor beams are 54 inches in your are elected to the in it. I the versional parts.

What Bracing.

The operator of ind bracina are to be found on PLATE IX. The upper letter 1 years in of the Carron type. The members are made up of the argue 12000. The lower external system is made up of the area by but it has additional mub-diagonal and struts which give support to the lower chard members widenly between panel values. The horizontal length of one post into three parts and help to support all the diagonals and verticals which they intersect. The sway bracing but a nogetical chainsts of horizontal struts between points where the langitudinal struts, just mentioned, intersect the posts and of diagonal members.

The letails of the and-bearings are given on PLATE X.

- Jamuel Kuin.

C.C. Grifinhagen.

May 16th 1906













